

Summer 2008 Physics 262, Exam 3: SOLUTIONS

Section A

1. D	5. C	9. C	13. A	17. B	21. A
2. C	6. D	10. A	14. A	18. D	22. C
3. B	7. C	11. A	15. C	19. A	23. D
4. D	8. A	12. B	16. D	20. B	

Section B

1. Water has a specific heat of $4 \times 10^3 \text{ J}/(\text{kg} \cdot \text{C}^\circ)$ and latent heat of fusion of $3.3 \times 10^5 \text{ J}/\text{kg}$. If I mix 1.0 kg of water at 33°C with 1.0 kg of ice at 0°C in a thermally insulated container, how much ice has melted when the mixture comes to thermal equilibrium? Recall that ice melts at 0°C . [Hint: To simplify the calculation, first figure out the *algebraic expression* for the amount of ice that is melted, then insert the numbers given.]

Answer:

Use conservation of energy: $Q_{\text{water}} + Q_{\text{ice}} = 0$, where Q is positive when heat is absorbed, and negative when heat is released. The heat absorbed by the water as it cools from 33°C to 0°C is

$$Q_{\text{water}} = m_{\text{water}} c_{\text{water}} \Delta T,$$

and the heat absorbed by the ice as it changes its phase to water is

$$Q_{\text{ice}} = m_{\text{ice}} L.$$

Conservation of energy gives

$$m_{\text{water}} c_{\text{water}} \Delta T + m_{\text{ice}} L = 0 \Rightarrow m_{\text{ice}} = -\frac{m_{\text{water}} c_{\text{water}} \Delta T}{L}.$$

The final mixture will have ice and water at 0°C . Substituting in the numbers given in the problem

$$\begin{aligned} m_{\text{water}} &= 1.0 \text{ kg} \\ c_{\text{water}} &= 4 \times 10^3 \text{ J}/(\text{kg} \cdot \text{C}^\circ), \\ \Delta T &= 0^\circ\text{C} - 33^\circ\text{C} = -33^\circ\text{C} \\ L &= 3.3 \times 10^5 \text{ J}/\text{kg}, \end{aligned}$$

gives the mass of the ice that melts,

$$m_{\text{ice}} = -\frac{(1.0 \text{ kg}) \cdot (4 \times 10^3 \text{ J}/(\text{kg} \cdot \text{C}^\circ)) \cdot (-33^\circ\text{C})}{3.3 \times 10^5 \text{ J}/\text{kg}} = \frac{(4 \times 10^3) \cdot 33}{33 \times 10^4} \text{ kg} = \boxed{0.4 \text{ kg}}.$$

2. For which of the following transitions in a hydrogen atom is the wavelength of the emitted light the *longest*? (1) $n = 2$ to $n = 1$ (2) $n = 3$ to $n = 1$ (3) $n = \infty$ to $n = 2$. Justify your answer quantitatively (that is, with numbers).

Answer:

The energy of the photon E_{photon} is given by conservation of energy, $E_{\text{photon}} + \Delta E = 0 \Rightarrow E_{\text{photon}} = -\Delta E$, where ΔE is the change in energy of the hydrogen atom. The energy levels of the hydrogen atom are $E_n = -E_R/n^2$, where $E_R = 13.6 \text{ eV}$ and n are integers.

(1) For $n = 2 \rightarrow n = 1$, $\Delta E = -E_R \left(\frac{1}{1^2} - \frac{1}{2^2} \right) = -\frac{3}{4}E_R \Rightarrow E_{\text{photon}} = \frac{3}{4}E_R$.

(2) For $n = 3 \rightarrow n = 1$, $\Delta E = -E_R \left(\frac{1}{1^2} - \frac{1}{3^2} \right) = -\frac{8}{9}E_R \Rightarrow E_{\text{photon}} = \frac{8}{9}E_R$.

(3) For $n = \infty \rightarrow n = 2$, $\Delta E = -E_R \left(\frac{1}{2^2} - \frac{1}{\infty^2} \right) = -\frac{1}{4}E_R \Rightarrow E_{\text{photon}} = \frac{1}{4}E_R$.

Since $E_{\text{photon}} = hf = hc/\lambda$, the photon with the lowest energy has the longest wavelength. Since $\frac{1}{4} < \frac{3}{4} < \frac{8}{9}$, the lowest energy and longest wavelength photon corresponds to:

$$\boxed{(3) \ n = \infty \text{ to } n = 2 \text{ transition}}.$$