

Physics For Life Sciences 2: Exam 2 Solutions

Section A

1. D	5. D	9. B	13. D	17. B	21. B
2. B	6. B	10. C	14. A	18. A	22. D
3. C	7. B	11. A	15. C	19. B	23. A
4. B	8. D	12. B	16. A	20. A	

Section B

Question 1: A $+4 \times 10^{-9}$ C point charge is at $x = 2$ m and a -1×10^{-9} C point charge is at $x = -3$ m. What is the electric field at $x = 0$ m due to these two charges? (Include the correct sign in your answer; *i.e.*, “+” and “-” for the electric field pointing in the positive and negative x -directions, respectively.)

Answer:

The electric field at a point due to charge q_i is

$$\mathbf{E} = \frac{kq_i}{r_i^2} \hat{\mathbf{r}},$$

where r_i is the distance of the charge to the point and $\hat{\mathbf{r}}$ is the unit vector pointing from the charge to the point.

The electric fields due to each of the two charges at the origin are

$$+4 \times 10^{-9} \text{ C charge : } \frac{9 \times 10^9 \text{ Nm}^2/\text{C}^2 \cdot (4 \times 10^{-9} \text{ C})}{(2 \text{ m})^2} \times \underbrace{(-1)}_{\substack{\text{unit vector in} \\ -x\text{-direction}}} = -9 \text{ N/C};$$

$$-1 \times 10^{-9} \text{ C charge : } \frac{9 \times 10^9 \text{ Nm}^2/\text{C}^2 \cdot (-1 \times 10^{-9} \text{ C})}{(3 \text{ m})^2} \times \underbrace{(+1)}_{\substack{\text{unit vector in} \\ +x\text{-direction}}} = -1 \text{ N/C}.$$

The electric field at the origin is the sum of these electric fields:

$$\mathbf{E}_{\text{at origin}} = -9 \text{ N/C} - 1 \text{ N/C} = \boxed{-10 \text{ N/C}}.$$

Questions 2: You have 3 resistors of resistances $1\ \Omega$, $\frac{1}{2}\ \Omega$ and $\frac{1}{4}\ \Omega$.

- (a) What is the equivalent resistance when you connect all three resistors in **series**? [8 points]
- (b) What is the equivalent resistance when you connect all three resistors in **parallel**? [12 points]

Answers:

(a)

$$R_{\text{equiv}} = \sum_i R_i = 1\ \Omega + \frac{1}{2}\ \Omega + \frac{1}{4}\ \Omega = \boxed{1\frac{3}{4}\ \Omega}.$$

(b)

$$\frac{1}{R_{\text{equiv}}} = \sum_i \frac{1}{R_i} = \frac{1}{1\ \Omega} + \frac{1}{\frac{1}{2}\ \Omega} + \frac{1}{\frac{1}{4}\ \Omega} = \frac{1+2+4}{\Omega} = \frac{7}{\Omega} \Rightarrow R_{\text{equiv}} = \boxed{\frac{1}{7}\ \Omega}.$$